

2.3 Answers

A-Level Pure Mathematics : Year 1 GCSE (Grades 8 and 9) Algebra of Surds and Indices I

2.3.1 Solutions (2.1 Example)

Method 1 : Less Mathematical

$$\begin{aligned} & 2 \sqrt{15} \times 4 \sqrt{10} \\ &= 2 \times \sqrt{3} \times \sqrt{5} \times 4 \times \sqrt{2} \times \sqrt{5} \\ &= 2 \times 4 \times (\sqrt{5} \times \sqrt{5}) \times \sqrt{3} \times \sqrt{2} \\ &= 8 \times 5 \times \sqrt{3} \times \sqrt{2} \\ &= 40\sqrt{6} \end{aligned}$$

Method 2 : More Mathematical

$$\begin{aligned} & 2 \sqrt{15} \times 4 \sqrt{10} \\ &= 8 \times \sqrt{150} \\ &= 8 \times \sqrt{25 \times 6} \\ &= 8 \times 5 \times \sqrt{6} \\ &= 40\sqrt{6} \end{aligned}$$

[2 marks]

2.3.2 Solutions to 2.2 Exercise

Answer 1

$$\begin{aligned} \text{(i)} & 63\sqrt{14} \\ \text{(iii)} & 80\sqrt{33} \end{aligned}$$

$$\begin{aligned} \text{(ii)} & 20\sqrt{35} \\ \text{(iv)} & 60\sqrt{22} \end{aligned}$$

[8 marks]

Answer 2

$$\begin{aligned} \text{(i)} & 2\sqrt{3} \\ \text{(iv)} & 3\sqrt{5} \\ \text{(vii)} & 5\sqrt{3} \\ \text{(x)} & 5\sqrt{5} \end{aligned}$$

$$\begin{aligned} \text{(ii)} & 2\sqrt{5} \\ \text{(v)} & 4\sqrt{3} \\ \text{(viii)} & 9\sqrt{2} \\ \text{(xi)} & 9\sqrt{7} \end{aligned}$$

$$\begin{aligned} \text{(iii)} & 2\sqrt{2} \\ \text{(vi)} & 11\sqrt{2} \\ \text{(ix)} & 7\sqrt{3} \\ \text{(xii)} & 4\sqrt{7} \end{aligned}$$

[12 marks]

Answer 3

$$\begin{aligned} \text{(i)} & 15\sqrt{2} \\ \text{(iv)} & 12\sqrt{5} \end{aligned}$$

$$\begin{aligned} \text{(ii)} & 20\sqrt{3} \\ \text{(v)} & 20\sqrt{7} \end{aligned}$$

$$\begin{aligned} \text{(iii)} & 15\sqrt{6} \\ \text{(vi)} & 14\sqrt{5} \end{aligned}$$

[6 marks]

Answer 4

$$\begin{aligned} \text{(i)} & \sqrt{11} \\ \text{(iv)} & 3\sqrt{3} \end{aligned}$$

$$\begin{aligned} \text{(ii)} & \sqrt{6} \\ \text{(v)} & 3\sqrt{2} \end{aligned}$$

$$\begin{aligned} \text{(iii)} & 2\sqrt{2} \\ \text{(vi)} & 5\sqrt{2} \end{aligned}$$

[6 marks]

Answer 5

(i) 7

(ii) 10

(iii) 3

[3 marks]**Answer 6**

(i) $\sqrt{2}$

(ii) $\sqrt{2}$

(iii) $2\sqrt{2}$

[3 marks]**Answer 7**

(i) $19\sqrt{3}$

(ii) $10\sqrt{2}$

(iii) $3\sqrt{5}$

(iv) $25\sqrt{6}$

[8 marks]**Answer 8**

(i) $15\sqrt{7}$

(ii) $70\sqrt{2}$

(iii) $60\sqrt{6}$

(iv) $6\sqrt{10}$

(v) $55\sqrt{15}$

(vi) $144\sqrt{2}$

[6 marks]**Answer 9**

(i) $6 + 5\sqrt{7}$

(ii) $1 + 5\sqrt{2}$

(iii) $3 + 4\sqrt{6}$

(iv) $4 + 2\sqrt{10}$

(v) $6 - 11\sqrt{15}$

(vi) $4 + 16\sqrt{2}$

[12 marks]**Answer 10**

(i) $40 + 6\sqrt{10}$

(ii) $-2 + \sqrt{22}$

(iii) $1 + 3\sqrt{39}$

[6 marks]