

7.5 Answers

Additional Mathematics
A-Level Pure Mathematics : Year 1
Topics in Algebra

7.5.1 Solution to 7.2 Example (Introductory Example)

(i) $y = (x - 7)^2 - 3$

(ii) $(7, -3)$ (iii) -3 (iv) 7

[4 marks]

7.5.2 Solutions to 7.3 Exercise

Answer 1

(i) $y = (x - 4)^2 - 11$ (ii) $(4, -11)$ (iii) -11

[3 marks]

Answer 2

$$D = 12^2 - 4 \times 3 \times 19 = -84$$

As this is negative the graph does not cross the x-axis.

[2 marks]

Answer 3

(i) $y = (x + 5)^2 - 7$ (ii) $(-5, -7)$ (iii) -5

[3 marks]

Answer 4

$$\begin{aligned} 3x^2 + 12x + 19 &= 3[x^2 + 4x] + 19 \\ &= 3[(x + 2)^2 - 4] + 19 \\ &= 3(x + 2)^2 - 12 + 19 \\ &= 3(x + 2)^2 + 7 \end{aligned}$$

$$\therefore p = 3, q = 2 \text{ and } r = 7$$

[3 marks]

Answer 5

(i) 11 (ii) $\frac{3}{8}$ (iii) -1 (iv) $-\frac{3}{4}$

[4 marks]

Answer 6

(i) 8 (ii) $\frac{2}{5}$ (iii) -2.4 (iv) 8

[4 marks]

Answer 7

$$\begin{aligned}
(\sqrt{k} - 1)^2 &\geq 0 \\
k - 2\sqrt{k} + 1 &\geq 0 \\
k + 1 &\geq 2\sqrt{k} \\
\frac{k+1}{\sqrt{k}} &\geq 2 \quad \square
\end{aligned}$$

[4 marks]**Answer 8**

(i) $y = 3(x + 5)^2 + 1$ (ii) $(-5, 1)$ (iii) 1

[3, 1, 1 marks]**Answer 9**

$$\begin{aligned}
x^2 + (2k + 3)x + k^2 + 3k + 1 &= 0 \\
D &= (2k + 3)^2 - 4 \times 1 \times (k^2 + 3k + 1) \\
&= 4k^2 + 12k + 9 - 4k^2 - 12k - 4 > 0 \\
&= 5
\end{aligned}$$

As the discriminant is positive the quadratic equation
has two distinct real roots $\square$

[4 marks]**Answer 10**

(i) $y = \left(x + \frac{1}{2}\right)^2 + \frac{3}{4}$ (ii) $\left(-\frac{1}{2}, \frac{3}{4}\right)$ (iii) $-\frac{1}{2}$

[3 marks]**Answer 11**

Knowing the binomial theorem is helpful although the question can be done without.
The coefficient matching technique will be new to some students.

$$\begin{aligned}
(x - A)^3 - 4 &= x^3 - 6x^2 + 12x + B \\
x^3 - 3x^2A + 3xA^2 - A^3 - 4 &= x^3 - 6x^2 + 12x + B \\
\therefore 3A &= 6 \Rightarrow A = 2 \\
-A^3 - 4 &= B \Rightarrow B = -12
\end{aligned}$$

[5 marks]

Answer 12

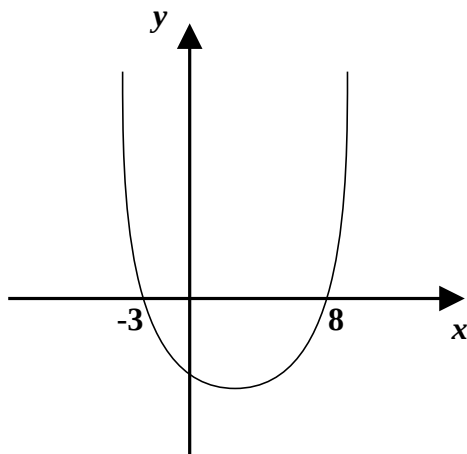
(i) $y = (x + 3)(x - 8)$

[1 mark]

(ii) $(-3, 0), (8, 0)$

[2 marks]

(iii)



[2 marks]