

3.5 Answers

3.5.1 Solution to 3.2 Exercise

Answer 1

$$(i) \quad \frac{7}{3} \Rightarrow 3 \overline{)7} \Rightarrow 3 \overline{)7}^{\text{r } 1} \Rightarrow 2 + \frac{1}{3}$$

$$\frac{7}{3} = 2\frac{1}{3}$$

[2 marks]

$$(ii) \quad \frac{56}{5} \Rightarrow 5 \overline{)56} \Rightarrow 5 \overline{)56}^{\text{r } 1} \Rightarrow 11 + \frac{1}{5}$$

$$\frac{56}{5} = 11\frac{1}{5}$$

[2 marks]

$$(iii) \quad \frac{93}{4} \Rightarrow 4 \overline{)93} \Rightarrow 4 \overline{)93}^{\text{r } 1} \Rightarrow 23 + \frac{1}{4}$$

$$\frac{93}{4} = 23\frac{1}{4}$$

[2 marks]

$$(iv) \quad \frac{31}{7} \Rightarrow 7 \overline{)31} \Rightarrow 7 \overline{)31}^{\text{r } 3} \Rightarrow 4 + \frac{3}{7}$$

$$\frac{31}{7} = 4\frac{3}{7}$$

[2 marks]

Answer 2

$$(i) \quad 4\frac{2}{5} = 4 + \frac{2}{5}$$

$$= \frac{4}{1} \times \textcolor{red}{1} + \frac{2}{5} \quad \text{Because } 4 = \frac{4}{1} \times 1$$

$$= \frac{4}{1} \times \textcolor{red}{5} + \frac{2}{5} \quad \text{Lesson 1 technique}$$

$$= \frac{20}{5} + \frac{2}{5} \quad \text{Lesson 1 technique}$$

$$= \frac{22}{5} \quad \text{Lesson 1 technique}$$

[2 marks]

(ii)

$$\begin{aligned} 9\frac{3}{4} &= 9 + \frac{3}{4} \\ &= \frac{9}{1} \times \mathbf{1} + \frac{3}{4} \\ &= \frac{9}{1} \times \frac{\mathbf{4}}{\mathbf{4}} + \frac{3}{4} \\ &= \frac{36}{4} + \frac{3}{4} \\ &= \frac{39}{4} \end{aligned}$$

Because $9 = \frac{9}{1} \times 1$

Lesson 1 technique

Lesson 1 technique

Lesson 1 technique

[2 marks]

(iii)

$$\begin{aligned} 50\frac{5}{6} &= 50 + \frac{5}{6} \\ &= \frac{50}{1} \times \mathbf{1} + \frac{5}{6} \\ &= \frac{50}{1} \times \frac{\mathbf{6}}{\mathbf{6}} + \frac{5}{6} \\ &= \frac{300}{6} + \frac{5}{6} \\ &= \frac{305}{6} \end{aligned}$$

Because $50 = \frac{50}{1} \times 1$

Lesson 1 technique

Lesson 1 technique

Lesson 1 technique

[2 marks]

(iv)

$$\begin{aligned} 108\frac{1}{3} &= 108 + \frac{1}{3} \\ &= \frac{108}{1} \times \mathbf{1} + \frac{1}{3} \\ &= \frac{108}{1} \times \frac{3}{3} + \frac{1}{3} \\ &= \frac{324}{3} + \frac{1}{3} \\ &= \frac{325}{3} \end{aligned}$$

Because $108 = \frac{108}{1} \times 1$

Lesson 1 technique

Lesson 1 technique

Lesson 1 technique

[2 marks]

3.5.2 Solution to 3.4 Exercise

Answer 1

$$\begin{aligned} \text{(i)} \quad 8\frac{3}{11} &= \frac{8 \times 11 + 3}{11} \\ &= \frac{88 + 3}{11} \\ &= \frac{91}{11} \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad 15\frac{2}{3} &= \frac{15 \times 3 + 2}{3} \\ &= \frac{45 + 2}{3} \\ &= \frac{47}{3} \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad 7\frac{9}{10} &= \frac{7 \times 10 + 9}{10} \\ &= \frac{70 + 9}{10} \\ &= \frac{79}{10} \end{aligned}$$

$$\begin{aligned} \text{(iv)} \quad 25\frac{3}{4} &= \frac{25 \times 4 + 3}{4} \\ &= \frac{100 + 3}{4} \\ &= \frac{103}{4} \end{aligned}$$

[8 marks]

Answer 2

$$\text{(i)} \quad \{\text{Multiples of 6}\} = \{6, 12, \mathbf{18}, 24, 30, 36, \dots\}$$

[1 mark]

$$\text{(ii)} \quad \{\text{Multiples of 9}\} = \{9, \mathbf{18}, 27, 36, 45, 54, \dots\}$$

[1 mark]

$$\text{(iii)} \quad \text{lcm}\{6, 9\} = 18$$

[1 mark]

$$\begin{aligned} \text{(iv)} \quad 3\frac{5}{6} - 2\frac{5}{9} &= \frac{3 \times 6 + 5}{6} - \frac{2 \times 9 + 5}{9} \\ &= \frac{23}{6} \times \mathbf{1} - \frac{23}{9} \times \mathbf{1} \\ &= \frac{23}{6} \times \frac{\mathbf{3}}{\mathbf{3}} - \frac{23}{9} \times \frac{\mathbf{2}}{\mathbf{2}} \\ &= \frac{69}{18} - \frac{46}{18} \\ &= \frac{23}{18} \\ &= 1\frac{5}{18} \end{aligned}$$

Use $\text{lcm}\{6, 9\}$ is 18

[8 marks]

Answer 3

(i) {Multiples of 4} = {4, 8, 12, 16, **20**, 24, ...}

[1 mark]

(ii) {Multiples of 10} = {10, **20**, 30, 40, 50, 60, ...}

[1 mark]

(iii) $lcm\{4, 10\} = 20$

[1 mark]

(iv) $5\frac{3}{4} + 3\frac{3}{10} = \frac{5 \times 4 + 3}{4} + \frac{3 \times 10 + 3}{10}$
 $= \frac{23}{4} \times \mathbf{1} + \frac{33}{10} \times \mathbf{1}$
 $= \frac{23}{4} \times \frac{\mathbf{5}}{\mathbf{5}} + \frac{33}{10} \times \frac{\mathbf{2}}{\mathbf{2}}$ Use $lcm\{4,10\}$ is 20
 $= \frac{115}{20} + \frac{66}{20}$
 $= \frac{181}{20}$
 $= 9\frac{1}{20}$

[8 marks]